A Leslie-type urban-rural migration model, and the situation of Germany and Turkey

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Abstract

Movements in the age structure of a population are often accompanied by substantial rural-urban migration. It is therefore compelling to analyze the implications of fertility, mortality, and migration patterns together. A joint Leslie-type population model of urban and rural populations is used to project the current population structure into the future, allowing for migration in both directions. This model permits an analysis of the long-run (stable) population properties, such as urbanization, under the assumption that current conditions persist, as well as an analysis of rural and urban populations in isolation, when migration is computationally eliminated. Applying the model to the female populations below age 50 of Germany and Turkey, it is found that the actual urbanization is lower (higher) than long-run urbanization in Germany (Turkey, respectively). The slight long-run growth of the Turkish population is due to rural-urban migration, while Turkish urban areas have a below-replacement fertility.

Keywords: Leslie-type model; urban-rural migration; stable population theory; population growth; urbanization; Germany and Turkey

1 Introduction

"The world is undergoing the largest wave of urban growth in history", the United Nations Population Fund warns in an 2007 online release.¹ Meanwhile, by the year 2010, world urbanization has arrived at the 50% level, with a five-year urban population growth of 1.9% (compared to an

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¹http://www.unfpa.org/pds/urbanization.htm. Accessed May 2011

overall population growth of 1.2%), which is an aggregate of values spanning from 0.7 for more developed regions to 4.0 for least-developed countries, according to the UNFPA State of World Population report 2010 (UNFPA, 2010).

Urbanization and economic growth are often closely linked, but urbanization concentrates poverty as well. Urbanization results from internal migration. Therefore, on the other hand, the increasing urbanization is insofar problematic as it contributes to the aggravation of the structural weakness of rural regions which may just be a major push factor of rural-urban migration. Urbanization may also be linked to decreasing fertility and shrinking, hence ageing populations, as there is a gap in fertility levels between urban and rural regions throughout the world.² Population structures of Germany and Turkey are compared, the former "developed" with respect to urbanization as well as growth, and the latter also "developed" with respect to urbanization, but "less developed" with respect to growth, according to UNFPA (2010).

Germany, among the more developed countries, is attributed a 74% level of urbanization in UNFPA (2010), along with an indiscernible urban growth (the reported growth rate is (0.0%) within five years. Accelerated urbanization in Germany became apparent from the midnineteenth century onward; it had its origin in industrialization and its impulse to the formation of new urban settlements (which, according to Köllmann (1969), became possible only with the abolition of the older municipal constitutions of "guild and trade restrictions designed to discourage migration"). Tracing the trends of internal migration in German history, Mai et al. (2007) distinguish a phase of long-distance migration (from rural areas in the East to urban areas in the West), progressively replacing migration from urban hinterland, so that by the early twentieth century about 50% of the German population had become internal migrants, as Köllmann (1976) calculates. Between the wars, for reasons of supply and ideology, beginnings of a trend back to the countryside could be observed. When the World War II aftermath with its reallocation of population had abated in the late 1950s, a phase of suburbanization solidified in Western Germany, leading to the emergence of urban sprawls and a persisting large-scale deconcentration of population. However, rural-urban migration remained relevant particularly for the young. — The situation in East Germany before 1990 was different, where regional concentration of population had prevailed. A sharp drop in younger age groups could be witnessed in the 1990s, which was triggered in particular by east-west migration after German reunification and amplified by low fertility rates; Flöthmann (1994), Mai et al. (2007). Thus, suburbanization trends in East Germany have attenuated by now, with urban sprawls gradually coming into being.

The ongoing phenomenon of rural depopulation used to hit east-German regions in particular, but not exclusively. It is selective with respect to the younger age of migrants, and is accompanied by low total fertility levels (1.33 in 2010; UNFPA, 2010) having persisted for more than three decades. Mai et al. (2007) assert that total growth of the German population today rests solely on an increase in life expectancy, the ageing of the population being notably pronounced in rural areas.

With a 70% proportion of population living in urban areas today, Turkey is on a level with more developed regions like Germany, while its five-year urban growth rate of 1.9% is characteristic for less-developed countries according to UNFPA (2010). With delay from the trend in Germany, urbanization in Turkey started on a large scale in the early 1950s from a level of 20% only. For the Turkish population between 1955 and 2000, Gedik (2003) investigated the Alonso theory of differential urbanization which postulates cycles of three evolutionary phases, urbanization, polarization reversal, and counter urbanization, where growth rates are highest for large, medium, and small settlement sizes, respectively. Gedik found evidence for a phase of pre-concentration in small cities in the 1950s, large-city urbanization that followed, and polarization "dispersal" starting in 1980 with highest growth rates in medium-sized cities dispersed throughout the country.

Simultaneously, Turkey experienced a pronounced change in fertility. Within three decades, the total fertility rate halved down to barely 2 today (2.09 in 2010; UNFPA, 2010). The Turkey Demographic and Health Survey 2008 (Hacettepe University Institute of Population Studies, 2008) investigates fertility preferences and behavior of Turkish women by residence, and provides information on maternal and child health. Among the findings is that, though total urban fertility is below replacement and the urban-rural differential appears to be contracting over time, clear above-replacement levels in South and East Anatolia persist. At each age class, rural women tend to bear more children than women in urban centers where a trend that fertility decreases with a higher educational level can be observed. As a result, the urban-rural gap with respect to the median age at first birth is broadening. A significantly higher proportion in urban centers of women in the working ages certainly adds to this gap, and thus the effects of rural-to-urban migration of economically active women. Furthermore, the findings of the survey indicate a significant urban-rural differential in child mortality which appears to be correlated with the mother's young age and educational level.

From a formal point of view, the phenomenon of urbanization (respectively rural depopulation) can be analyzed as a result of migration probabilities and their interaction with urbanand rural-specific fertility rates and survival probabilities. The approach may vary in several basic respects: The focus may be either on forecasting the future population using forecasts of mortality, fertility and migration, or on population projection in order to find answers to what the population would be like in the long run if mortality, fertility and migration would evolve (or persist) in a certain way. The effects of demographic and environmental conditions on the dynamics of populations may be studied in discrete or continuous time, in a deterministic framework, or using a probabilistic model with random variation in births, deaths, and migration.

In her overview of probabilistic approaches to demographic and population forecasting, Booth (2006) identifies three widely-used frameworks: methods on the basis of sample data on individual expectations about future developments or expert opinions, structural modeling methods based on theories on relations between demographic variables and processes, and extrapolative methods using time series models to detect patterns and trends in the past and extrapolate them into the future. A time series approach recently adopted by Hyndman and Booth (2008) involves functional data models to forecast mortality, fertility, and migration.

The Leslie population model (in recognition of Leslie's work; Leslie, 1945) falls under the category of projection. In its classical formulation, it is a discrete-time and age-structured (respectively stage-structured; Lefkovitch, 1965) transition matrix model for the evolution of a closed population in time, but can be extended to a Leslie-type model which allows for immigration; for example, Feichtinger and Steinmann (1990), Schmidbauer and Rösch (1995). The spectral properties of the matrix provide insight into asymptotic population growth rates and stable stage structures. A detailed review of matrix population models, including Leslie models for populations in time-varying, deterministic or stochastic environments, is given by Caswell (2001). Many applications and developments in spatial demography have their root in the (also matrix-based) multiregional cohort-component model introduced by Rogers (1966, 1995), which, accessing a multispatial life table, describes the dynamics of a population which is dispersed over different spatial patches and allows for migration in between. An example is the multi-

regional multinational cohort-component projection model by Kupiszewska and Kupiszewski; Kupiszewska and Kupiszewski (2005) developed a revised form to capture international migration. For an ecological system in a multi-patch stochastic environment with different time scales for migration and vital rates, recently Alonso and Sanz (2009) showed the application of an aggregation method in order to obtain a reduced stochastic Leslie model.

Our contribution is a mathematical model conceived for urban and rural populations, which is an extension of the classical Leslie model and allows for migration from rural to urban areas and in the opposite direction. It can be understood as a particular formulation of the multiregional model by Rogers (1995) installing two regional types, urban and rural, but at the same time two kinds of inhabitants, natives and migrants. It is able to project the current urbanization structure into the future and permits sensitivity analyses of the influence of different vital patterns and migration scenarios on population growth and urbanization, as well as insight into the trade-off between fertility, mortality and migration with respect to stability.

This model is introduced in Section 2. First, a hypothetical population is considered in Section 3, then an application to the populations of Germany and Turkey is presented in Section 4. Finally, a summary is given and some suggestions for further research are discussed in Section 5. A further challenge was to obtain the information needed as input to the model. The data used, including data sources and data processing, are specified in the Appendix. All computations are carried out in R (R development core team, 2011).

2 The model

Our model deals with four populations of females: city natives, village natives, and two classes of migrants which are distinguished by destination into city migrants and village migrants. Time proceeds in discrete steps; for illustration purposes 15-year steps are used in this and the following section (but 5-year steps when applied to Germany and Turkey in Section 4). Accordingly, the four populations are structured by three 15-year intervals of age covering reproductive ages. The age-specific fertility, mortality and migration patterns are assumed to be constant through time. They may be village- or city-specific. In particular, the migrants' vital rates may differ from those of the natives as well, while second generation migrants are assumed to behave like natives with this respect; they are counted as natives actually.

Our model is defined by the relationship and the matrix displayed in Table 1; all symbols

($M_{I}^{[\text{city native}]}_{[\text{city native}]}$	$M_{I}^{[ext{city migrant}]}_{[ext{city native}]}$	$M_{I}^{[\text{village native}]}_{[\text{city native}]}$	$M_{I_{\text{[city native]}}^{[\text{village migrant]}}}$	
	$M_{I}^{[\text{city native}]}_{[\text{city migrant}]}$	$M_{I}^{[\text{city migrant}]}_{[\text{city migrant}]}$	$M_{I}^{[\text{village native}]}_{[\text{city migrant}]}$	$M_{I}^{[\text{village migrant}]}_{[\text{city migrant}]}$	(1)
	$M_{I}^{[\text{city native}]}_{[\text{village native}]}$	$M_{I}^{[\text{city migrant}]}_{[\text{village native}]}$	$M_{I}^{[\text{village native}]}_{[\text{village native}]}$	$M_{I}^{[\text{village migrant}]}_{[\text{village native}]}$	(-)
	$M_{I[\text{village migrant}]}$	$M_{I}^{[\text{city migrant}]}_{[\text{village migrant}]}$	$M_{I}^{[\text{village native}]}_{[\text{village migrant}]}$	$M_{I}^{[\text{village migrant}]}$)

are defined in Table 2. Schematically, the matrix M_I can also be written as

with sub-matrices $M_{I_{\text{[to]}}}^{\text{[from]}}$ indicating possible transitions within one time step. Such a submatrix will be a zero matrix whenever the corresponding transition is impossible (as in the case $M_{I_{\text{[city mative]}}}$). The element-by-element sum of submatrices along a column of the partitioned M_{I} will result in a usual Leslie matrix, which in turn defines population streams channeled to several possible destinations by means of the migration pattern.

Theorem: Consider an age-structured population evolving according to $N_t = M_I \cdot N_{t-1}$. Let the following conditions be satisfied: (i) migration probabilities from city to village and from village to city are positive for any (not necessarily the same) age class, (ii) survival probabilities are all positive, and (iii) fertility rates are positive for any two adjacent age classes. Then:

a) There exists a stable population structure \tilde{N} and a $\lambda \in \mathbb{R}$ such that

$$\lambda \cdot \tilde{N} = M_I \cdot \tilde{N}. \tag{2}$$

Here, λ is the maximum eigenvalue of M_I .

- b) The future long-run growth rate of an initial population is given by the maximum eigenvalue of M_I .
- c) All four population segments (city native, city migrant, village native, village migrant) will ultimately grow with the same rate.

Proof: The projection matrix M_I is a non-negative square matrix, irreducible and primitive. Therefore, classical Perron-Frobenius theory can be applied; for example, Seneta (1981) and Caswell (2001).

Irreducibility and primitivity can be evaluated from the transition diagrams in Figures 1 and 2: The "life cycle graph" is strongly connected, i.e. each pair of nodes is connected in the sense that one node can be reached from the other within a finite number of transitions. The greatest common divisor of loop lengths is 1. This holds if only the conditions of the theorem are satisfied.

Then, according to the Perron-Frobenius theorem, there exists a real and positive eigenvalue λ which dominates any other eigenvalue of M_I . The eigenvectors associated to λ are strictly positive and unique to constant multiples. In particular, there exists a right eigenvector \tilde{N} such that equation (2) holds. It follows what is known as the strong ergodic theorem, that λ completely determines the long-term dynamics of the population:

$$\lim_{t \to \infty} \frac{N_t}{\lambda^t} = c \cdot \tilde{N} \tag{3}$$

In the long run, the population will grow at a rate given by λ , with a stable population structure proportional to \tilde{N} . In particular, this ultimate growth rate carries over to all four population segments.

$\langle n_{c1,t-1} \rangle$	$n_{c2,t-1}$	$n_{c3,t-1}$	$\overline{n^*_{c1,t-1}}$	$n^{st}_{c2,t-1}$	$n_{c3,t-1}^{st}$	$\frac{1}{n_{v1,t-1}}$	$n_{v2,t-1}$	$n_{v3,t-1}$	$n^*_{v1,t-1}$	$n^{st}_{v2,t-1}$	$\langle n_{v3,t-1}^* \rangle$
0	0	0	$f_{v3}^{*}m_{v3}^{*}$	0	0	$f_{v3}^*\bar{m}_{v3}^*$	0	0	0	0	0
0	0	0	$f_{v2}^*m_{v2}^*$	0	$p_{v2}^{st}m_{v2}^{st}$	$f_{v2}^* \bar{m}_{v2}^*$	0	0	0	0	$p_{v2}^*\bar{m}_{v2}^*$
0	0	0	$f_{v1}^*m_{v1}^*$	$p_{v1}^{*}m_{v1}^{*}$	0	$f_{v1}^*ar{m}_{v1}^*$	0	0	0	$p_{v1}^*ar{m}_{v1}^*$	0
0	0	0	$f_{v3}m_{v3}$	0	0	$f_{v3} \bar{m}_{v3}$	0	0	0	0	0
0	0	0	$f_{v2}m_{v2}$	0	$p_{v2}m_{v2}$	$f_{v2}\bar{m}_{v2}$	0	$p_{v2} \bar{m}_{v2}$	0	0	0
0	0	0	$f_{v1}m_{v1}$	$p_{v1}m_{v1}$	0	$f_{v1}\bar{m}_{v1}$	$p_{v1} \bar{m}_{v1}$	0	0	0	0
$f_{c3}^* ar{m}_{c3}^*$	0	0	0	0	0	0	0	0	$f_{c3}^{*}m_{c3}^{*}$	0	0
$f_{c2}^*\bar{m}_{c2}^*$	0	0	0	0	$p^*_{c2} \bar{m}^*_{c2}$	0	0	0	$f_{c2}^{*}m_{c2}^{*}$	0	$p_{c2}^{st}m_{c2}^{st}$
$f_{c1}^* \bar{m}_{c1}^*$	0	0	0	$p_{c1}^* ar{m}_{c1}^*$	0	0	0	0	$f_{c1}^{*}m_{c1}^{*}$	$p_{c1}^{\ast}m_{c1}^{\ast}$	0
$f_{c3} ar{m}_{c3}$	0	0	0	0	0	0	0	0	$f_{c3}m_{c3}$	0	0
$f_{c2} \bar{m}_{c2}$	0	$0 p_{c2} ar{m}_{c2}$	0	0	0	0	0	0	$f_{c2}m_{c2}$	$p_{c1}m_{c1}$ 0	$p_{c2}m_{c2}$
$f_{c1}\bar{m}_{c1}$	$p_{c1} ar{m}_{c1}$	0	0	0	0	0	0	0	$f_{c1}m_{c1}$	$p_{c1}m_{c1}$	0
					I						
$\langle n_{c1t} \rangle$	n_{c2t}	n_{c3t}	$\overline{n_{c1t}^*}$	n_{c2t}^*	n_{c3t}^*	n_{v1t}	n_{v2t}	n_{v3t}	n^*_{v1t}	n^*_{v2t}	$\langle n^*_{v3t} \rangle$
	city native {		Ļ	city migrant \langle			village native			village migrant \langle	_

Table 1: The relation $N_t = M_I \cdot N_{t-1}$

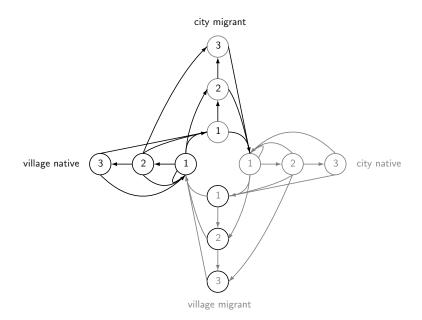


Figure 1: Transitions between states (except migrant to migrant transitions)

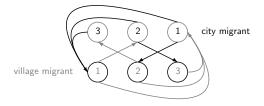


Figure 2: Transitions between migrant states

3 A hypothetical example

The following hypothetical example is meant to illustrate the dynamics of the model outlined in Section 2, and to demonstrate how the model can contribute to analyzing the successive development of a population. The example is based on a population broken down into three 15-year age classes: 0–15, 15–30 and 30–45. The first step in constructing the population dynamics is to define two Leslie matrices describing two populations, "city" and "village", in isolation (with no migration between them). The two populations are then linked together by specifying fertility rates and survival probabilities for migrants and, most crucially, a migration pattern between them. In what follows, two among many possible migration patterns will be investigated with respect to the stable development of the resulting population. When analyzing actual populations, the migration pattern has to be inferred from population statistics, and in this case the procedure of linking populations together can be reversed to study city and village populations in isolation, as will be seen in Section 4.

Symbol	Definition
f_{ci}	the average number of girls born to a native of city in age class i , and surviving to the next age class
f_{vi}	the average number of girls born to a native of village in age class i , and surviving to the next age class
f_{ci}^*	the average number of girls born to a migrant (from village to city) is age class i , and surviving to the next age class
f_{vi}^*	the average number of girls born to a migrant (from city to village) is age class i , and surviving to the next age class
p_{ci}	the probability that a native of city now in age class i , survives to b in $i + 1$
p_{vi}	the probability that a native of village now in age class i , survives to b in $i + 1$
p_{ci}^*	the probability that a migrant (from village to city) now in age class survives to be in $i+1$
p_{vi}^*	the probability that a migrant (from city to village) now in age class survives to be in $i+1$
m_{ci}	probability that a city native in age group i migrates to village
\bar{m}_{ci}	probability that a city native in age group i does not migrate to village $\bar{m}_{ci} = 1 - m_{ci}$
m_{vi}	probability that a village native in age group i migrates to city
\bar{m}_{vi}	probability that a village native in age group i does not migrate to city $\bar{m}_{vi} = 1 - m_{vi}$
m_{ci}^*	probability that a migrant (from village to city) in age group i migrate again (back to village)
\bar{m}_{ci}^*	probability that a migrant (from village to city) in age group i does not migrate again (back to village); $\bar{m}_{ci}^* = 1 - m_{ci}^*$
m_{vi}^*	probability that a migrant (from city to village) in age group i migrate again (back to city)
\bar{m}_{vi}^*	probability that a migrant (from city to village) in age group i does no migrate again (back to city); $\bar{m}_{vi}^* = 1 - m_{vi}^*$
n_{ct}	age structured city population of natives in period t
n_{vt}	age structured village population of natives in period t
n_{ct}^*	age structured population of migrants from village to city in period \boldsymbol{t}
n_{vt}^*	age structured population of migrants from city to village in period t

Table 2: Explanation of symbols in the model

3.1 Two populations in isolation

Let two Leslie matrices be given as

$$M_{\rm city} = \begin{pmatrix} 0.10 & 0.20 & 0.20 \\ 0.95 & 0 & 0 \\ 0 & 0.90 & 0 \end{pmatrix}, \quad M_{\rm village} = \begin{pmatrix} 0.30 & 0.90 & 0.70 \\ 0.90 & 0 & 0 \\ 0 & 0.85 & 0 \end{pmatrix}. \tag{4}$$

Their respective maximum eigenvalues are: $\lambda_{city} = 0.7086$, $\lambda_{village} = 1.2699$. The resulting growth of the stable populations in a 15-year interval is therefore -29.14% (city) and +26.99%(village), corresponding to annual rates of -2.27% and +1.61%, respectively. When considered in isolation, the city population is thus shrinking, while the village population is growing (when stability is reached). The next step is to link the two populations together through specification of a migration pattern between them. The two cases considered are: (i) there is no further migration after migrating once, (ii) migration is location-specific.

3.2 Linkage I: no migration back to the origin

The assumptions connecting city and village populations are:

• Assumption 1: Migration probabilities may depend on the origin (city or village), but are equal across age classes:

$$m_{c1} = m_{c2} = m_{c3} = m_c, \quad m_{v1} = m_{v2} = m_{v3} = m_v.$$
 (5)

• Assumption 2: A migrant will stay at her destination and won't migrate back:

$$m_{c1}^* = m_{c2}^* = m_{c3}^* = 0, \quad m_{v1}^* = m_{v2}^* = m_{v3}^* = 0.$$
 (6)

• Assumption 3: Migrants' survival probabilities are obtained as arithmetic means of city native and village native survival probabilities in their respective age class:

$$p_{ci}^* = p_{vi}^* = 0.5 \cdot (p_{ci} + p_{vi}), \quad i = 1, 2, 3.$$
(7)

• Assumption 4: As far as fertility is concerned, migrants will "split the difference" between city and village fertility, that is, the age-specific fertility rate of migrants is obtained as the arithmetic mean of the respective age-specific fertility rates of city and village population. In symbols:

$$f_{ci}^* = f_{vi}^* = 0.5 \cdot (f_{ci} + f_{vi}), \quad i = 1, 2, 3.$$
(8)

This leads to the matrix M_I displayed in Table 3. A comparison of the matrices M_I in Tables 1

($0.10\bar{m}_c$	$0.20\bar{m}_c$	$0.20\bar{m}_c$	0.20	0.55	0.45	0	0	0	0	0	0)
1	$0.95\bar{m}_c$	0	0	0	0	0	0	0	0	0	0	0
L	0	$0.90\bar{m}_c$	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	$0.30m_v$	$0.90m_v$	$0.70m_v$	0	0	0
L	0	0	0	0.90	0	0	$0.90m_v$	0	0	0	0	0
	0	0	0	0	0.85	0	0	$0.85m_v$	0	0	0	0
l	0	0	0	0	0	0	$0.30\bar{m}_v$	$0.90\bar{m}_v$	$0.70\bar{m}_v$	0.20	0.55	0.45
l	0	0	0	0	0	0	$0.90\bar{m}_v$	0	0	0	0	0
L	0	0	0	0	0	0	0	$0.85\bar{m}_v$	0	0	0	0
L	$0.10m_{c}$	$0.20m_c$	$0.20m_c$	0	0	0	0	0	0	0	0	0
	$0.95m_c$	0	0	0	0	0	0	0	0	0.95	0	0
ĺ	0	$0.90m_c$	0	0	0	0	0	0	0	0	0.90	0 /

Table 3: Matrix M_I , resulting from the assumptions in the example

and 3 reveals that $M_{I}^{\text{[city migrant]}}_{[village migrant]}$ and $M_{I}^{[village migrant]}_{[city migrant]}$ are now zero matrices, reflecting the assumption that migration back is impossible ($m_c^* = m_v^* = 0$). Considering the growth properties of city (shrinking) and village (growing) populations, the theorem in Section 2 implies that there is a migration pattern, expressed by m_c and m_v , that will ultimately lead to a *stationary* total population. The transient behavior of the population is illustrated in Figure 3, with plots of the 12 series (four population groups: native city, migrant city, native village, migrant village; each broken down into three age groups) in $N_t = M_I \cdot N_{t-1}$ for $t = 1, \ldots, 25$, where the initial population is given by

$$N'_{0} = (\underbrace{1000, 1000, 1000}_{\text{city native}}, \underbrace{0, 0, 0}_{\text{city migrant}}, \underbrace{1000, 1000, 1000}_{\text{village native}}, \underbrace{0, 0, 0}_{\text{village migrant}}), \tag{9}$$

and with migration probabilities $m_c = 0.1$ (from city to village) and $m_v = 0.3$ (from village to city) The maximum eigenvalue of M_I , as displayed in Table 3, equals $\lambda = 0.9920$, so that the population shrinks in the long run: The low fertility of the city population prevails due to the

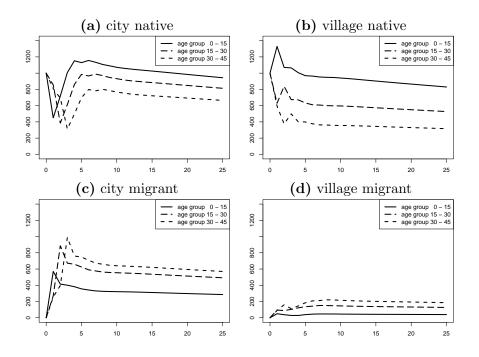


Figure 3: Evolution of initial population

high village-to-city migration ($m_v = 0.3$). Lowering m_v somewhat (to $m_v = 0.28$, say) would make the population grow.

In which way do growth and urbanization of the population in the long run depend on fertility? This question can be discussed by letting stable growth and urbanization depend on two factors, designated as f_c factor and f_v factor in Figure 4, with which fertility rates f_{ci} , f_{ci}^* and f_{vi} , f_{vi}^* , respectively, are multiplied. This method of investigating the influence of fertility is suitable because fertility rates have no theoretical upper bound. Figure 4 shows the contour lines of growth (that is, the maximum eigenvalue of M_I , hence the growth in a 15-year interval) and urbanization when city-specific and village-specific fertility rates are varied in a range from -50% to +100% of their original levels (Table 3).

Urbanization is computed as the share of population in the first six components of the population vector. (Technically, urbanization is the sum of the first six components of the right eigenvector belonging to the maximum eigenvalue, divided by the total sum.) The higher slope of the growth surface along the f_v factor axis points to the more important role of *village* fertility for growth under the given mortality and migration regime. A higher village fertility can offset a higher city fertility with respect to urbanization, at the same time leading to higher growth.

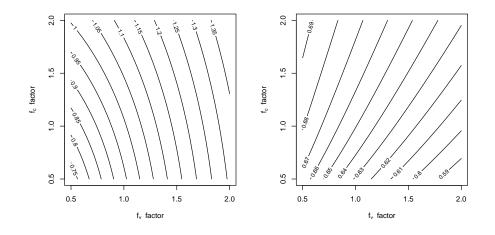


Figure 4: Influence of fertility on growth (left) and urbanization (right), example

3.3 Linkage II: location-specific migration probabilities

Only a single migration is possible for each person under Assumption 2 above. The two Leslie matrices in (4) can also be linked together such that the maximum number of two migrations in a model with three age groups (nine migrations in a model with ten age groups, see Section 4 below) become possible. One way to achieve this is by replacing Assumption 2 with

• Assumption 2': A migrant adopts the migration pattern of her current location:

$$m_{ci}^* = m_{ci}, \quad m_{vi}^* = m_{vi}, \quad i = 1, 2, 3.$$
 (10)

This amounts to making migration probabilities location-specific in the sense that the status of a potential migrant is irrelevant.

The long-run influence of migration probabilities on growth and urbanization can be studied using the matrix M_I in Table 3, whose structure will now be modified by letting long-run growth and long-run urbanization be a function of $m_v \equiv m_{vi}$ and $m_v \equiv m_{vi}$. In contrast to the procedure when investigating the influence of fertility, a new set of migration probabilities is substituted, m_c and m_v , rather than multiplying by a factor, because a probability is bounded by one. Plots of resulting contour lines are displayed in Figure 5. In particular, a higher city-tovillage migration can offset a higher village-to-city migration in terms of equal long-run growth, where the ratio depends on the location of (m_v, m_c) . For example, high village-to-city migration will lead to below-replacement overall fertility if city-to-village migration is low (the lower right corner of the left-hand plot in Figure 5). At the same time, urbanization will approach a high

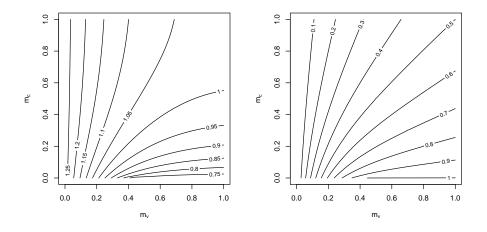


Figure 5: Influence of migration on growth (left) and urbanization (right)

level (the lower right corner of the right-hand plot).

4 Analyzing the populations of Germany and Turkey

The goal of this section is to analyze the populations of Germany and Turkey on the basis of the model defined in Section 2. Data concerning age structure, fertility, survival, and migration are presented in the Appendix. The first step will be to give an account of the assumptions made to obtain the projection matrix M_I . This will enable us to compare the actual populations of Germany and Turkey with their respective stable counterparts, and to discuss the influence of fertility and migration levels on long-run growth and urbanization, similar to the procedure undertaken in Section 3.

4.1 Definition of M_I

The subsequent analysis is based on ten five-year age groups, covering ages 0 to 50. All data used in the definition of M_I are reported in the Appendix. On this basis, the entries of the projection matrix M_I (see Table 1) are obtained as follows:

- Natives' fertility rates f_{ci} , f_{vi} , survival probabilities p_{ci} , p_{vi} , and migration probabilities are taken from Table 7 (Germany) and Table 8 (Turkey).
- Migrants' probabilities to migrate again are obtained as indicated in Assumption 2' in Section 3, that is: migration probabilities m_{ci}^* and m_{vi}^* are location-specific.
- Migrants' survival probabilities p_{ci}^{\ast} and p_{vi}^{\ast} are obtained as arithmetic means of city native

and village native survival probabilities in their respective age class; this is Assumption 3 in Section 3.

• Migrants' fertility rates f_{ci}^* and f_{vi}^* are obtained as arithmetic means of city native and village native fertility rates in their respective age class; this is Assumption 4 in Section 3.

4.2 Actual and stable populations

Given the initial population N_0 and the projection matrix M_I , the model permits a comparison of actual and stable populations in terms of numerical characteristics (Table 4) and in terms of histograms of age distributions in Figures 6 and 7.

	Gerr	nany	Tur	key
	actual	stable	actual	stable
urbanization	85.3%	87.5%	65.0%	58.7%
growth, city, annual	-1.0806%	-1.2748%	0.894%	0.302%
growth, village, annual	-1.8154%	-1.2748%	1.239%	0.302%
total growth, annual	-1.1874%	-1.2748%	1.015%	0.302%
median age, city	29.53	28.85	21.81	24.42
median age, village	29.40	28.64	19.75	22.66

Table 4: Characteristics of (female) populations, age 0–50: actual and stable

City and village populations at time t can be obtained by adding native and migrant parts of the vector N_t ; urbanization is the share of total population belonging to the city part. Growth measures referring to the actual population result from relating the initial population N_0 to $N_1 = M_I \cdot N_0$; for the stable population, the maximum eigenvalue of M_I equals the growth factor, and stable growth must be equal for all population parts. The median age is found using linear interpolation of cumulative age group frequencies. Median age here refers to the female population aged 0–50.

In the case of Germany, actual village population shrinks much faster than it would in the case of stability. Median age is very similar in city and village; it is lower in for the stable population. This is confirmed by the age distributions shown in Figure 6: the actual population of Germany is older than its stable counterpart. Frequencies of the stable population in the histograms are essentially increasing, which is a consequence of the population being shrinking, but there is an exception: the slight trough in village population, age group 25–30, is due to migration.

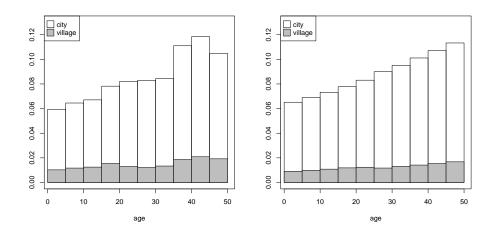


Figure 6: Actual (left) and stable (right) female population of Germany

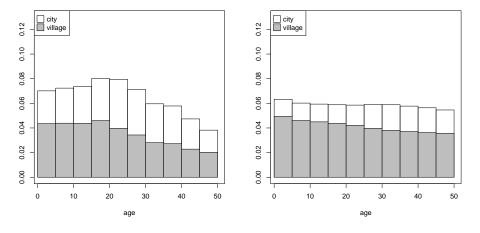


Figure 7: Actual (left) and stable (right) female population of Turkey

The actual Turkish growth figures in Table 4 reflect the young age structure of the population when compared to its stable counterpart, which is also obvious from Figure 7. The relation between city and village with respect to urbanization and median age is the opposite of that in Germany, actual median age being lower than stable median age. The hump (age groups 25–35) in the otherwise monotonically decreasing histogram frequencies in the case of the city age distribution is again due to migration.

4.3 City and village populations in isolation

Partitioning the projection matrix M_I according to (1) reveals the characteristics of city and village population if there were no migration. Projection matrices for the populations evolving

	Germany	Turkey
maximum eigenvalue, $M_{I,city}$	0.9375	0.9954
maximum eigenvalue, $M_{I,\text{village}}$	0.9412	1.0385
growth, city in isolation, annual	-1.2829%	-0.0922%
growth, village in isolation, annual	-1.2057%	0.7587%
median age, city in isolation	28.85	24.90
median age, village in isolation	28.61	22.30

Table 5: Populations characteristics, age 0–50, without migration

in isolation are obtained as

$$M_{I,\text{city}} = M_{I}^{[\text{city native}]}_{[\text{city native}]} + M_{I}^{[\text{city native}]}_{[\text{village migrant}]},$$

$$M_{I,\text{village}} = M_{I}^{[\text{village native}]}_{[\text{village native}]} + M_{I}^{[\text{village native}]}_{[\text{city migrant}]}.$$
(11)

(Computationally removing migration in this way creates a situation which is similar to the starting point in Section 3.) The projection matrices $M_{I,\text{city}}$ and $M_{I,\text{village}}$ can be analyzed like a classical Leslie matrix. A comparison of the models characteristics in isolation, as given in Table 5, with the characteristics of the full model (Table 4) will then reveal the balancing effect of migration. For example, long-run growth in Turkish cities arises only through migration, while internal fertility is below replacement level. The difference in city and village fertility is much smaller in the case of Germany. The diminished mitigating effect of migration in Germany is also reflected in the smaller difference between city and village median age.

A further interpretation of growth rates of city and village in isolation is that any migration pattern, with which $M_{I,\text{city}}$ and $M_{I,\text{village}}$ are linked together (see Section 3), will lead to an overall stable growth between the values of city and village growth.

4.4 Influence of fertility levels on growth and urbanization

As in Section 3.2, stable growth and urbanization can be plotted as functions of factors with which city fertility $f_c \equiv (f_{c,1}, \ldots, f_{c,10})$ and village fertility $f_v \equiv (f_{v,1}, \ldots, f_{v,10})$ are multiplied. The result is displayed in Figures 8 and 9 where these factors, designated as f_c factor and f_v factor respectively, range from 0.5 to 2.0, corresponding to lowering fertility levels down to 50% and increasing them up to 200% of actually observed levels. We proceed with migrants' fertility according to Assumption 4 above. "Growth" in Figures 8 and 9 refers to five-year intervals.

There is a substitution effect between city and village fertility, which is more or less constant

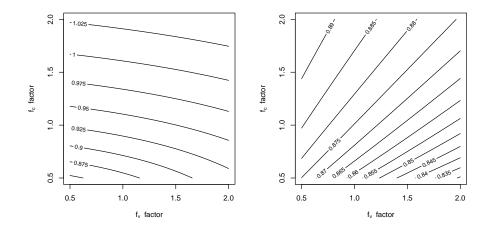


Figure 8: Influence of fertility levels on growth (left) and urbanization (right), Germany

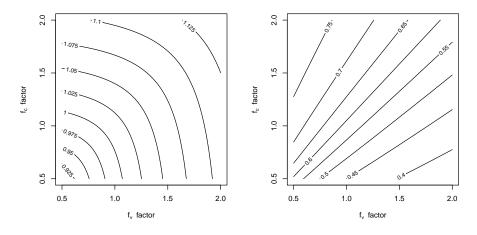


Figure 9: Influence of fertility levels on growth (left) and urbanization (right), Turkey

across the factor range considered for the population in Germany, but not Turkey, where the importance of village fertility increases in a non-linear fashion as city fertility falls below village fertility. This substitution has a big influence on urbanization, with urbanization contour lines standing almost perpendicular to growth contour lines. The shape of urbanization contour lines is very similar for Germany and Turkey.

Fertility levels in Germany are well below replacement level. For example, with village fertility unchanged (f_v factor = 1), it can be shown that city fertility would have to be raised by about 61% in order to reach replacement level.

4.5 Influence of migration on growth and urbanization

The influence of migration probabilities m_c and m_v on growth and fertility is shown in Figures 10 and 11. The procedure used to modify the projection matrix M_I is as explained in Section 3.3. As stated earlier, five-year growth will be between that indicated by the maximum eigenvalues of city and village population in isolation (given in Table 5). The influence of the balance between m_v and m_c on urbanization can be grave when both probabilities are small, according to the right-hand plots in Figures 10 and 11. Contour line shapes are similar for the populations of Germany and Turkey, but with growth again at different levels.

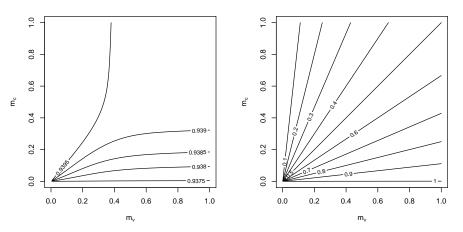


Figure 10: Influence of migration on growth (left) and urbanization (right), Germany

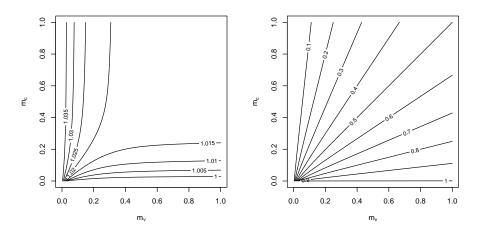


Figure 11: Influence of migration on growth (left) and urbanization (right), Turkey

5 Summary and conclusions

We use a projection-matrix based population model which takes rural-urban and urban-rural migration explicitly into consideration. Perron-Frobenius theory provides insight into the stable behavior of this model. This approach constitutes a platform for the analysis of the influence of fertility rates, survival probabilities, as well as migration patterns on long-run characteristics of a population. The interplay between fertility, mortality and migration, in particular: how village and city populations are connected together through migration, is illustrated using hypothetical examples.

Applying this model to the female populations of Germany and Turkey, as represented by their respective age structures, fertility rates, and survival and migration probabilities in 5year age intervals up to age 50, insight could be obtained in two ways: (i) comparing actual population characteristics with their stable counterparts; (ii) analyzing the stable behavior of city and village populations in isolation, when migration is computationally removed from the populations.

In Germany, both actual and stable, city as well as village actual populations are shrinking. The strongest actual negative growth (-1.8% annually) is observed for the village population, which is substantially greater than in the case of the stable growth (-1.3%); the rapid depopulation of rural areas (relative to urban areas) in Germany thus appears as a transient phenomenon. Median age of actual populations is slightly higher than in stable populations: the actual population of Germany is actually older than is would be in the long run, if current demographic parameters persist. Long-run urbanization levels were found to be very similar to its current level, if slightly higher.

Turkish population characteristics differ from those of the German population in almost every respect. Current population growth is positive and higher than in stability (+0.3% annually), and highest (+1.2% annually) in the case of the actual village population. Median age of the city population is markedly higher than of the village population, and stable median age is higher than the actual median age (which explains the currently higher growth rate): the current young population structure of Turkey is, in this sense, a transient phenomenon, and so is the high level of urbanization, which will recede in in the long run if current demographic parameters persist.

When considered in isolation, little difference was found between stable characteristics of city and village populations of Germany, while the stable city population of Turkey was found to shrink, to the effect that the slight overall population increase of Turkey is due to migration. It was also found that a slight change in migration patterns can have a profound influence on long-run urbanization in Germany as well as in Turkey.

The framework on which this study is based provides ample opportunity for further research. Two directions are: (i) to elaborate further characteristics of actual populations, and assess the influence of public policies on the future population structure and its economic consequences, such as the age dependency ratio; (ii) to gain further theoretical insight into the model, for example, the transformation of the model into a Markov chain (this was found useful for other Leslie-type models; for example, Schmidbauer and Rösch, 1995), which would create a platform for the introduction of reproductive values in order to study migration and fertility from a novel perspective.

Appendix: Data for Germany and Turkey

	Germ	lany	Turkey			
age group	city	village	city	village		
0-4	1495604	258293	1980044	1208088		
5 - 9	1623683	294710	2052625	1218246		
10 - 14	1687545	314490	2090782	1217217		
15 - 19	1967756	388228	2254619	1263638		
20 - 24	2065329	327007	2204497	1058935		
25 - 29	2086654	306365	2000720	918105		
30 - 34	2121947	336474	1693854	763431		
35 - 39	2792868	469649	1652431	748377		
40 - 44	2979696	525380	1356984	628241		
45 - 49	2637994	483548	1097967	560045		

Table 6 shows the initial female city and village populations of Germany and Turkey.

Table 6: The initial (female) age-structured populations of Germany and Turkey

Germany

All data referring to the population of Germany were obtained on the basis of data retrieved from German official databases, namely "Regionaldatenbank Deutschland"³ providing regional data, and "GENESIS-Online"⁴ providing data on the federal level.

Definition of city/village population. The *city population* is the population living outside of "rural areas". The definition of *rural* areas used here adopts the OECD urban-rural

 $^{^3 \}rm Official$ Statistics Federal Republic of Germany, Düsseldorf, Regional
datenbank Deutschland. URL http://www.regional
statistik.de. Accessed March 2012

⁴Federal Statistical Office, Wiesbaden, GENESIS-Online. URL https://www-genesis.destatis.de/genesis/online. Accessed March 2012

typology (OECD, 2007). In a first step, local administrative units (LAU2, "Gemeinden, Samt-/Verbandsgemeinden") were labeled *rural* if their population density was below 150 inhabitants per square kilometer. NUTS 3 regions ("Kreise, kreisfreie Städte"), at the next higher territorial level, provided the data used for the projection matrix M_I . For the purposes of this study, they are classified as *rural* if the share of regional population living in rural LAU2 regions is more than 50% and if there were no urban centers with more than 200 000 inhabitants accounting for at least 25% of the population. The base year of this definition is 2008. The population living in rural (respectively predominantly rural) areas defined in this way constitutes what is called "village population" in Germany. All further data were aggregated on the basis of this territorial typology.

End-year 2005 population data serve as the initial female city and village populations of Germany; cf. Table 6. (The two groups covering ages below 10 were defined by splitting and combining available age groups proportional to their respective lengths.) The share of female village population amounts to 14.7% at that time, with respect to the total female population (i.e. covering all ages classes).

Fertility. Female births during years 2006 through 2010 were aggregated by age groups of the mother and related to the average female population in those years to estimate five-year fertility rates. (Age groups "below 20 years" and "40 years and older" were treated as five-year intervals; fertility rates of beyond ages were set to 0.)

Mortality. Probabilities of surviving five years from the beginning of each age group were derived from the German life-table (years 2008 through 2010), abridging sets of one-year data. No effort is made here to differentiate between city- and village-specific survival probabilities.

Migration. Migration probabilities from city to village and vice versa, covering five years from the beginning of each age group, were estimated in several steps. In a first step, age-specific cases of female departure from (arrivals to) urban/rural areas were aggregated from reported data covering years 2006 through 2010, and adjusted for internal migration. Since departing from an urban area is not synonymous with arriving at a rural area, and neither the destination of departures nor the origin of arrivals was available, the share of arrivals to a rural area among all arrivals was used to obtain directional departures for each age group. Finally, migration probabilities were obtained by relating these results to the average female population, and applying Farr's method under the assumption that there is constant migration and that the

average sojourn time of a female who migrated within a time period of five years is 2.5 years.

fertility		$\operatorname{survival}$		migration		
rate		proba	bility	probability		
city	village	city	village	to city	to village	
0.0000	0.0000	0.9962	0.9962	0.0950	0.0165	
0.0000	0.0000	0.9996	0.9996	0.0942	0.0175	
0.0000	0.0000	0.9996	0.9996	0.0938	0.0179	
0.0224	0.0218	0.9991	0.9991	0.2376	0.0333	
0.0976	0.1101	0.9989	0.9989	0.4161	0.0455	
0.1943	0.2327	0.9987	0.9987	0.3389	0.0503	
0.2193	0.2182	0.9983	0.9983	0.0976	0.0157	
0.1049	0.0841	0.9973	0.9973	0.0966	0.0170	
0.0208	0.0148	0.9954	0.9954	0.0963	0.0175	
0.0000	0.0000	0.9916	0.9916	0.0957	0.0183	
	ra <u>city</u> 0.0000 0.0000 0.0224 0.0976 0.1943 0.2193 0.1049 0.0208	rate <u>city</u> village 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0224 0.0218 0.0976 0.1101 0.1943 0.2327 0.2193 0.2182 0.1049 0.0841 0.0208 0.0148	$\begin{array}{c ccccc} rate & proba \\ \hline city & village & city \\ \hline 0.0000 & 0.0000 & 0.9962 \\ \hline 0.0000 & 0.0000 & 0.9996 \\ \hline 0.0000 & 0.0000 & 0.9996 \\ \hline 0.0224 & 0.0218 & 0.9991 \\ \hline 0.0976 & 0.1101 & 0.9989 \\ \hline 0.1943 & 0.2327 & 0.9987 \\ \hline 0.2193 & 0.2182 & 0.9983 \\ \hline 0.1049 & 0.0841 & 0.9973 \\ \hline 0.0208 & 0.0148 & 0.9954 \\ \hline \end{array}$	rate probability city village city village 0.0000 0.0000 0.9962 0.9962 0.0000 0.0000 0.9996 0.9996 0.0000 0.0000 0.9996 0.9996 0.0000 0.0000 0.9996 0.9996 0.00224 0.0218 0.9991 0.9991 0.0976 0.1101 0.9989 0.9989 0.1943 0.2327 0.9987 0.9987 0.2193 0.2182 0.9983 0.9983 0.1049 0.0841 0.9973 0.9973 0.2028 0.0148 0.9954 0.9954	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

The resulting rates and probabilities are given in Table 7.

Table 7: German (female) population data used for the projection matrix M_I

Turkey

Various data sources were used: publications concerning the 2000 census by the Turkish Statistical Institute (2000, 2005); the Turkey Demographic and Health Survey 2003, conducted by the Hacettepe University Institute of Population Studies (2004) in Ankara; and the WHO database⁵.

Definition of city/village population. The notion of *city*, as defined by the Turkish Statistical Institute for the 2000 census of population (Turkish Statistical Institute, 2000), relates to province and district centers of Turkey (il ve ilçe merkezler), while the notion of village comprises sub-districts and villages (bucak ve köyler). The initial female city and village populations of Turkey refer to the outcome of this census and are shown in Table 6. The share of female village population amounted to 35.5.7% in 2000, with respect to the total female population (i.e. covering all ages classes).

Fertility. Age-specific fertility rates of the city and village population in Turkey (for the three years preceding the 2003 demographic survey) were published by the Hacettepe University Institute of Population Studies (2004). Five-year rates of female births were obtained by simple adjustments (multiplying by a factor of 2.5).

 $^{^5 \}rm WHO$ (2011), Global Health Observatory Data Repository. URL http://apps.who.int/ghodata. Accessed May 2011.

Mortality. Survival probabilities (for the year 2000) were taken from the WHO database 6 , abridging the first two age intervals. Since city- and village-specific survival probabilities were not available, we assume that survival probabilities are equal.

Migration. Migration data for the preceding five years were collected in the 2000 census of population and published by the Turkish Statistical Institute (2005). Substitutes for migration probabilities were obtained as the number of female migrants (village to city or city to village), divided by the total female population in that age group (again village or city, respectively).

	fert	ility	surv	vival	migration		
	ra	te	proba	ability	probability		
age group	city	village	city	village	to city	to village	
0–4	0.0000	0.0000	0.9574	0.9574	0.0500	0.0300	
5 - 9	0.0000	0.0000	0.9969	0.9969	0.0430	0.0284	
10 - 14	0.0000	0.0000	0.9979	0.9979	0.0455	0.0265	
15 - 19	0.1100	0.1180	0.9971	0.9971	0.0631	0.0335	
20 - 24	0.3150	0.4030	0.9962	0.9962	0.1020	0.0445	
25 - 29	0.3150	0.3950	0.9953	0.9953	0.0821	0.0402	
30 - 34	0.1780	0.2350	0.9940	0.9940	0.0531	0.0320	
35 - 39	0.0830	0.1200	0.9918	0.9918	0.0415	0.0272	
40 - 44	0.0280	0.0400	0.9883	0.9883	0.0328	0.0261	
45 - 49	0.0000	0.0150	0.9824	0.9824	0.0264	0.0274	

The resulting rates and probabilities are given in Table 8.

Table 8: Turkish (female) population data used for the projection matrix M_I

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⁶WHO (2011), l.c.

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